

Solutions

1a.

<div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;"> <p>Before $\xrightarrow{2u}$</p> </div> <div style="text-align: center;"> <p>\xleftarrow{u}</p> </div> </div> <p style="text-align: right; margin-right: 50px;">Correct use of NEL</p>	M1
$y - x = e(2u + u)$ o.e.	A1
CLM (\rightarrow): $3m(2u) + 2m(-u) = 3m(x) + 2m(y)$ ($\Rightarrow 4u = 3x + 2y$)	B1
Hence $x = y - 3eu$, $4u = 3(y - 3eu) + 2y$, $(u(9e + 4) = 5y)$	M1
Hence, speed of Q = $\frac{1}{5}(9e + 4)u$ AG	A1

1b. Either

$x = y - 3eu = \frac{1}{5}(9e + 4)u - 3eu$	M1
Hence, speed P = $\frac{1}{5}(4 - 6e)u = \frac{2u}{5}(2 - 3e)$ o.e.	A1
$x = \frac{1}{2}u = \frac{2u}{5}(2 - 3e) \Rightarrow 5u = 8u - 12eu, \Rightarrow 12e = 3$ & solve for e	M1
gives, $e = \frac{3}{12} \Rightarrow \underline{e = \frac{1}{4}}$ AG	A1

Or

Using NEL correctly with given speeds of P and Q	M1
$3eu = \frac{1}{5}(9e + 4)u - \frac{1}{2}u$	A1
$3eu = \frac{9}{5}eu + \frac{4}{5}u - \frac{1}{2}u$, $3e - \frac{9}{5}e = \frac{4}{5} - \frac{1}{2}$ & solve for e	M1
$\frac{6}{5}e = \frac{3}{10} \Rightarrow e = \frac{15}{60} \Rightarrow e = \frac{1}{4}$.	A1



Solutions

1a.

$x^2 = 21^2 + 2 \times 40 \times 9.8$	M1
$x = 35$	A1
$0 = y^2 - 2 \times 40 \times 9.8$	M1
$y = 28$ may be implied	A1
$e = 28/35$	M1
$e = 0.8$ aef	A1

1b.

$0.2 \times 28 - - 0.2 \times 35$ must be double negative	M1
$I = 12.6$	A1





1. Two spheres of the same radius with masses 2 kg and 3 kg are moving directly towards each other on a smooth horizontal plane with speeds 8 m s^{-1} and 4 m s^{-1} respectively. The spheres collide and the kinetic energy lost is 81 J. Calculate the speed and direction of motion of each sphere after the collision. **(12)**



Solutions

1.

$16 - 12 = 2x + 3y$	M1
$4 = 2x + 3y$ aef	A1
$\frac{1}{2} \cdot 2(8)^2 + \frac{1}{2} \cdot 3(4)^2$ or $\frac{1}{2} \cdot 2x^2 + \frac{1}{2} \cdot 3y^2$ or $\pm \frac{1}{2} \cdot 2(8^2 - x^2)$ or $\pm \frac{1}{2} \cdot 3(4^2 - y^2)$	B1
$\frac{1}{2} \cdot 2(8)^2 + \frac{1}{2} \cdot 3(4)^2 - \frac{1}{2} \cdot 2x^2 - \frac{1}{2} \cdot 3y^2 = 81$	M1
$2x^2 + 3y^2 = 14$ aef	A1
Attempt to eliminate x or y from a linear and a quadratic equation	M1
$15y^2 - 24y - 12 = 0$ or $10x^2 - 16x - 26 = 0$ aef	A1
Attempt to solve a three term quadratic	M1
$x = -1$ (or $x = 2.6$)	A1
$y = 2$ (or $y = -2/5$)	A1
$x = -1$ and $y = 2$ only	A1
speeds 1, 2 away from each other	A1



Solutions

1a.

$-7.84e = 7.84e - gt$ Uses a complete method to find t .	M1
$t = 1.6e$	A2

1b.

(a) $t_2 = 1.6e^2$	B1
(b) $t_3 = 1.6e^3$	B1

1c.

Time to first bounce is 0.8 s	B1
Identify total time is sum of a GP in e Indication of the sum of at least to term in e^4	B1
Equate 3.4 or 4.2 or 5 or 5.8 with attempt at use of formula for sum to infinity of a GP.	M1
$\frac{1.6e}{1-e} = 4.2$	A1
$e = 0.724$ Allow 21/29	A1



Solutions

1a.

$5m = mu + 4m$ cons. of mom.	M1
$u = 1$	A1
$e = (2-1)/5$	M1
$e = \frac{1}{5}$	A1

1b.

$I = 4m$	B1
\rightarrow to the right	B1

1c.

$4m = 5mv$	M1
$v = \frac{4}{5}$	A1
$\frac{4}{5} < 1$	B1

