

Solutions

1a.

$\left(\frac{3}{5}\right)^2 \times \frac{2}{5}$	M1
$= 0.0518$ (3sfs) or $\frac{162}{3125}$	(oe) A1

1b.

$\left(\frac{3}{5}\right)^4$	M1
$1 - \left(\frac{3}{5}\right)^4$	M1
$= 0.870$ (3 sfs) or $\frac{544}{625}$	(oe) A1

2a.

$0.8^2 \times 0.2$	M1
$= \frac{16}{125}$ or 0.128	A1

2b.

$0.8^2 \times 0.2 + 0.8^3 \times 0.2 + 0.8^4 \times 0.2$ 1 term omitted or wrong or extra	M2 (M1)
$= \frac{976}{3125}$ or 0.312 (3 sfs)	A1



Solutions

1a.

$\left(\frac{4}{5}\right)^4$ alone or $1 - \left(\frac{1}{5} + \frac{4}{5} \times \frac{1}{5} + \left(\frac{4}{5}\right)^2 \times \frac{1}{5} + \left(\frac{4}{5}\right)^3 \times \frac{1}{5}\right)$	M1
$= \frac{256}{625}$ or 0.410 (3 sfs)	(allow 0.41) A1

1b.

$1 \div \frac{1}{5}$ $= 5$	B1
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2a.

$P(X = 2) = p(1 - p) = 0.16$	M1
$p^2 - p + 0.16 = 0$ $p = \frac{1 \pm \sqrt{(-1)^2 - 4(0.16)}}{2} = \frac{1 \pm \sqrt{0.36}}{2} = \frac{1 \pm 0.6}{2}$ $p = 0.2$ or 0.8	M1
As $p < 0.5$, solution is $p = 0.2$	A1

2b.

$E(X) = \frac{1}{0.2} = 5$	B1
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2c.

$\text{Var}(X) = \frac{1-0.2}{0.2^2} = \frac{0.8}{0.04} = 20$	B1
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Solutions

1.

Negative Binomial, $p = 0.60$, $r = 5$ $P(X = 8) = {}^7C_4 \times 0.60^5 \times 0.40^3$	M1
$= 0.17418$	A1

2.

Negative Binomial, $p = 0.3$, $r = 2$ $P(X = 6) = {}^5C_1 \times 0.3^2 \times 0.7^4$	M1
$= 0.108045$	A1

3.

Negative Binomial, $p = 0.65$, $r = 3$ $P(X = 6) = {}^5C_2 \times 0.65^3 \times 0.35^3$	M1
$= 0.117745$	A1



Solutions

1.

$\binom{6}{1}(0.15)(0.85)^5(0.15)$	M1
$= 0.05990$	A1

1b.

$\frac{3}{0.15} = 20$	B1
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1c.

Probability that John wins a coconut in a game is constant	B1
Games are independent	B1

1d.

$\frac{r}{p} = 18$	B1
$\frac{r(1-p)}{p^2} = 36$	B1
$18(1-p) = 36p$	M1
$p = \frac{1}{3} > 0.15$	A1
Sue has the greater probability of winning a coconut game	A1



Solutions

1a.

$0.7^4 \times 0.3$ alone		M1
$= 0.0720$ (3 sf) or $\frac{7203}{100000}$	(oe)	A1

1b.

$(0.7 + 0.7^2 + 0.7^3) \times 0.3$ 1 term omitted or wrong or extra		M2 (M1)
$= 0.4599$ or 0.460 (3 sf) or $\frac{4599}{10000}$	(oe)	A1

2a.

$\left(\frac{1}{2}\right)^3$		M1
$= \frac{1}{8} = 0.125$		A1

2b.

$X \sim \text{Negative B}(3, 0.125)$		M1
$P(X = 6) = \binom{5}{2} \times (0.125)^3 \times (0.875)^3$		M1
$= 0.0131$ (4 d.p.)		A1

