



## Solutions

1a.

$P(X = 3) = \frac{e^{-3.5} \times (3.5)^3}{3!}$	<b>M1</b>
$= 0.216$	<b>A1</b>

1b.

$P(Y \geq 5) = 1 - P(Y \leq 4)$ $= 1 - 0.2851$	<b>M1</b>
$= 0.715$	<b>A1</b>

2a.

Let $X$ be the random variable the number power cuts. $X \sim \text{Po}(3)$	<b>B1</b>
$P(X = 7) = P(X \leq 7) - P(X \leq 6) \quad \text{or} \quad \frac{e^{-3} \times 3^7}{7!}$ $= 0.9881 - 0.9665$	<b>M1</b>
$= 0.0216$ awrt 0.0216	<b>A1</b>

2b.

b. $P(X \geq 4) = 1 - P(X \leq 3)$ $= 1 - 0.6472$	<b>M1</b>
$= 0.3528$ awrt 0.353	<b>A1</b>





## Solutions

1a.

For a 1-year period The number of A grades $\sim \text{Po}(3)$	
For a 5-year period The number of A grades $\sim \text{Po}(15)$	<b>B1</b>
$P(\text{Total A-grades} > 18)$ $= 1 - (\text{Total} \leq 18)$ $= 1 - 0.8195$	<b>M1</b>
$= 0.181$ WFW 0.180 to 0.181	<b>A1</b>

1bi.

$X + Y \sim \text{Po}(10)$	<b>B1</b>
$P(X + Y \leq 14) = 0.917$ AWFW 0.916 to 0.917	<b>M1 A1</b>

1bii.

$X$ and $Y$ are independent variables.	<b>E1</b>
----------------------------------------	-----------









## Solutions

1a.

Let $X$ be the random variable the number of games Connie loses. $X \sim B(9, 0.2)$	<b>B1</b>
$P(X \leq 3) - P(X \leq 2) = 0.9144 - 0.7382$ or $(0.2)^3(0.8)^6 \frac{9!}{3!6!}$	<b>M1</b>
$= 0.1762$ awrt 0.176	<b>A1</b>

1b.

$P(X \leq 4) = 0.9804$	awrt 0.98	<b>M1 A1</b>
------------------------	-----------	--------------

1c.

Mean = $60 \times 0.05$ $= 3$	<b>M1</b>
Variance = $60 \times 0.05 \times (1 - 0.05)$ $= 2.85, \frac{57}{20}$ oe	<b>M1</b>

1d.

Po(3) (Poisson)	<b>M1</b>
$P(X > 4) = 1 - P(X \leq 4)$ $= 1 - 0.8153$	<b>M1</b>
$= 0.1847$	<b>A1</b>







## Solutions

1a.

$P(X = 1) = 0.25e^{-0.25}$	<b>M1</b>
$= 0.1947$ awrt 0.195	<b>A1</b>

1b.

$X \sim \text{Po}(1.5)$	<b>B1</b>
$P(X > 2) = 1 - P(X \leq 2)$ $= 1 - 0.8088$	<b>M1</b>
$= 0.1912$ awrt 0.191	<b>A1</b>

1c.

$[\lambda = 300 \times 0.25 = 75]$ $X \sim N(75, 75)$ For normal approximation and correct mean Var ( $X$ ) = 75 or sd = $\sqrt{75}$ or awrt 8.66 (may be given if correct in standardisation formula)	<b>B1</b> <b>B1</b>
$P(X < 90) = P(X \leq \frac{89.5 - 75}{\sqrt{75}})$ $= P(Z \leq 1.6743\dots)$ Using either 89.5 or 88.5 Standardising using their mean and their sd, using [89.5, 88.5 or 89] and for finding correct area	<b>M1</b> <b>M1</b>
$= \text{awrt } 0.953 \text{ or } 0.952$	<b>A1</b>
<b>NB</b> use of Poisson gives an answer of 0.9498 and gains no marks	

